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### RFI Measurement & Analysis Techniques

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# **Presentation Overview**

**RFI Measurement and Analysis Techniques** 









### Introduction

Protection Levels & Measured Data

### Radio Astronomy Protection Levels

ITU-R RA.769 Continuum Spectral Line

### RFI Measurements

Commercial Standards Military Standards SKA Standards

### **RFI** Analysis

Applying Telescope Protection Levels to Measurements Bandwidth Compensation



### INTRODUCTION Protection Levels

& Measured Data

I. Haywood, F. Camilo et. al., Inflation of 430-parsec bipolar radio bubbles in the Galactic Centre by an energetic event, Nature, Vol. 573, pp. 235-237, 11 Sept. 2019

# Introduction

### **Applying Telescope Protection Levels to Measurement Data**



#### [3] SKA EMI/EMC Standards & Procedures

Measurements", 2003.

P. Dewdney, G.-H. Tan, H. Smith, T. Tzioumis and J. Jonas, *SKA EMI/EMC standards SKA EMI/EMC Standards, Related Procedures and Guidelines*, Document Number SKA-TEL-SKO-0000202, Rev 03, 2017-03-13.





### Introduction

**Applying Telescope Protection Levels to Measurement Data** 



RADIO ASTRONOMY PROTECTION LEVELS ITU-R RA.769-2 Continuum Spectral Line

# Radio Astronomy Protection Levels

**ITU-R RA.769** 



SARAS  $[dBm/Hz] = -17.2708 \log_{10}(f) - 192.0714$  for f < 2 GHz SARAS  $[dBm/Hz] = -0.065676 \log_{10}(f) - 248.8661$  for f  $\ge 2$  GHz



- Harmful interference defined as interference power, within a chosen BW, that would produce an error of 10% in the smallest power that can be detected by the receiver (based on radiometer equation)
- Integration time of 2000 s with appropriate antenna and receiver noise temperatures



# **Radio Astronomy Protection Levels**

**Resolution Bandwidth (#1)** 



SARAS  $[dBm/Hz] = -17.2708 \log_{10}(f) - 192.0714$  for f < 2 GHz SARAS  $[dBm/Hz] = -0.065676 \log_{10}(f) - 248.8661$  for f  $\ge 2$  GHz

- \*Continuum Protection Level: Resolution Bandwidth equal to 1% of centre frequency being observed
- Spectral Line Protection Level: Resolution Bandwidth equal to 0.001% of centre frequency being observed

\*In the case of ITU-R RA.769-2, the continuum receiver bandwidth is assumed to be the extent of the ITU primary allocated band for the radio astronomy service. Using a 1% receiver bandwidth is of the same order of magnitude as the ITU allocated bands.



### RFI MEASUREMENTS

Commercial Standards Military Standards SKA Standards

**Commercial Standards** 

- Radio Astronomy Protection Levels: Maximum PSD allowed for signal received through 0 dB side lobe or main-lobe as measured at the input to the LNA
- We are often interested in impact of devices not necessarily situated at antenna focus
- Measured levels need to be translated to the focus by some distance R



Figure 1: Radiated emissions from DUT equipment toward the radio telescope.



**Spatial & Temporal Variability** 

 Given the nature of RFI/EMI both spatial variability (extended vs \*\*small culprits) as well as temporal variability (continuous vs transient) need to be considered.

\*\*Small culprits are typically where the DUT is smaller than the antenna beam

- Spatial Variability
  - Measurements on Component Level ("small" culprits)
  - Measurements on System Level ("extended" culprits)
- Temporal Variability
  - Measurements of Continuous RFI
  - Measurements of EMI
  - Measurements of Transient RFI and EMI



**Commercial Standards** 

- Radiated emissions from **commercial EUT** are typically limited by:
  - \* Federal Communications Commission (FCC) in USA
  - \* International Special Committee on Radio Interference (CISPR) in Europe and South Africa
  - \* CISPR is a committee of the International Electrotechnical Committee (IEC)
- Commercial or Military Standards (MIL-STD) will typically prescribe:
  - 1. Resolution Bandwidth
  - 2. Receiver Detectors
  - 3. Measurement Distances
  - 4. Antenna Heights
  - 5. Allowable Emission Limits
  - 6. Allowable Susceptibility Limits



CISPR 11/22 Class A & B





**Resolutions Bandwidth (#2)** 



- Electric Field Strength [dBuV/m]
- Constant RBW over Frequency Range (120 kHz or 1 MHz)

- Power Spectral Density [dBm/Hz]
- Continuum: RBW = 1% of fc
- Spectral Line: RBW = 0.001% of fc



**Resolutions Bandwidth (#2)** 





### **Resolutions Bandwidths**



#### Instrument and Protection Levels RBWs

Figure 2: Instrument and Protection Levels Resolution Bandwidths



### **RFI Signal Characteristics :: Resolution Bandwidth (#3)**

- Narrowband vs. Wideband signals
- It will always be ideal to match your measurement bandwidth to that of the signal bandwidth





### **Resolution Bandwidths**

When characterising emissions from a DUT and determining the impact on a radio telescope receiver, the following bandwidths need to be considered:

1. Interference signal bandwidths:  $\Delta f_{sig}$ 

(for example a narrowband or wideband interference signal)

- 2. Measurement receiver bandwidths:  $\Delta f_{\text{meas}}$ (for example using a spectrum analyser with an RBW of 120 kHz as per CISPR 22 Class B, or RTA-3.6 channel width of 25 kHz)
- 3. Radio astronomy protection levels bandwidths:  $\Delta f_{\text{thresh}}$ (1% or 0.001% of the centre frequency for Continuum or Spectral Line observations respectively)



**Bandwidth Compensation Factor** 



	$\Delta f_{\rm meas} < \Delta f_{\rm thresh}$			$\Delta f_{\rm meas} > \Delta f_{\rm thresh}$	
Narrowband Signal $\Delta f_{ m sig} < \Delta f_{ m meas}$	$\eta_1 > 1$	$\Delta f_{\rm sig} < \Delta f_{\rm thresh}$	Narrowband Signal $\Delta f_{ m sig} < \Delta f_{ m thresh}$	$\eta_4 < 1$	$\Delta f_{\rm sig} < \Delta f_{\rm thresh}$
$\Delta f_{\rm meas} \leq \Delta f_{\rm sig} < \Delta f_{\rm thresh}$	$\eta_2 > 1$	$\Delta f_{ m sig} < \Delta f_{ m thresh}$	$\Delta f_{\rm thresh} \leq \Delta f_{\rm sig} < \Delta f_{\rm meas}$	$\eta_5 < 1$	$\Delta f_{\rm sig} \geq \Delta f_{\rm thresh}$
Wideband Signal $\Delta f_{ m sig} \geq \Delta f_{ m thresh}$	$\eta_3 = 1$	$\Delta f_{\rm sig} \geq \Delta f_{\rm meas}$	Wideband Signal $\Delta f_{ m sig} \geq \Delta f_{ m meas}$	$\eta_6 = 1$	$\Delta f_{\rm sig} \geq \Delta f_{\rm thresh}$

Table 1: Various combinations of signal, instrument and protection level bandwidths will result in a different

bandwidth compensation factor ( $\eta$ ).



### Bandwidth Compensation Factor :: $\Delta f_{meas} < \Delta f_{thresh}$

 $\Delta f_{meas} < \Delta f_{thresh}$ 





Bandwidth Compensation Factor ::  $\Delta f_{meas} > \Delta f_{thresh}$ 

 $\Delta f_{meas} > \Delta f_{thresh}$ 





#### **Mathematical Derivation**

If a signal is band-limited and assumed to have a rectangular power spectral density  $PSD_{sig}(f)$  centered on a frequency  $f_0$ , then its PSD is:

$$PSD_{sig}(f) = \begin{cases} \frac{P_{sig}}{\Delta f_{sig}} & f_0 - \frac{\Delta f_{sig}}{2} \le f \le f_0 + \frac{\Delta f_{sig}}{2} & [dBm/Hz] \\ 0 & otherwise \end{cases}$$
(1)

When making a measurement of the spectrum of a signal, the power value ( $P_{meas}$ ) recorded at a frequency sample  $f_0$  is equal to the integral of the *intrinsic* signal power spectral density ( $PSD_{sig}(f)$ ) multiplied by the channel bandpass response ( $|H(f)|^2$ ):

$$P_{\text{meas}}(f_0) = \int_{-\infty}^{+\infty} |H(f)|^2 \cdot PSD_{\text{sig}}(f+f_0) \cdot df \quad [W]$$
(2)

This equation can be considered to be the convolution of the signal *PSD*<sub>sig</sub> with the bandpass response of the measuring device. Approximating the bandpass response to be rectangular, this can be simplified to:

$$P_{\text{meas}}(f_0) \approx \int_{f_0 - \frac{\Delta f_{\text{meas}}}{2}}^{f_0 + \frac{\Delta f_{\text{meas}}}{2}} PSD_{\text{sig}}(f) \cdot df \quad [W]$$
(3)



**Mathematical Derivation** 

Combining equations (1) and (3):

$$P_{\text{meas}}(f_0) \approx \begin{cases} \frac{P_{\text{sig}}}{\Delta f_{\text{sig}}} \int_{f_0 - \frac{\Delta f_{\text{sig}}}{2}}^{f_0 + \frac{\Delta f_{\text{sig}}}{2}} df = P_{\text{sig}} & \Delta f_{\text{sig}} \leq \Delta f_{\text{meas}} \\ \frac{P_{\text{sig}}}{\Delta f_{\text{sig}}} \int_{f_0 - \frac{\Delta f_{\text{meas}}}{2}}^{f_0 + \frac{\Delta f_{\text{meas}}}{2}} df = \left(\frac{\Delta f_{\text{meas}}}{\Delta f_{\text{sig}}}\right) \cdot P_{\text{sig}} & (\langle P_{sig} \rangle \mid \Delta f_{\text{sig}} > \Delta f_{\text{meas}} \end{cases}$$
(5)

which can be simplified to:

$$P_{\text{meas}}(f_0) \approx \min\left(1, \frac{\Delta f_{\text{meas}}}{\Delta f_{\text{sig}}}\right) P_{\text{sig}} \quad [W]$$
 (6)



**Mathematical Derivation** 

Combining equations (1) and (3):

$$P_{\text{meas}}(f_0) \approx \begin{cases} \frac{P_{\text{sig}}}{\Delta f_{\text{sig}}} \int_{f_0}^{f_0 + \frac{\Delta f_{\text{sig}}}{2}} df = P_{\text{sig}} & \Delta f_{\text{sig}} \leq \Delta f_{\text{meas}} \\ \frac{P_{\text{sig}}}{\Delta f_{\text{sig}}} \int_{f_0}^{f_0 + \frac{\Delta f_{\text{meas}}}{2}} df = \left(\frac{\Delta f_{\text{meas}}}{\Delta f_{\text{sig}}}\right) \cdot P_{\text{sig}} & ( \Delta f_{\text{meas}} \end{cases}$$
(5)

which can be simplified to:

$$P_{\text{meas}}(f_0) \approx \min\left(1, \frac{\Delta f_{\text{meas}}}{\Delta f_{\text{sig}}}\right) P_{\text{sig}} \quad [W]$$
 (6)

If the channel bandwidth of the measuring instrument is wider than the *intrinsic* signal bandwidth then the measured power at sample frequency  $f_0$  is equal to the total power of the signal, and independent of the channel bandwidth. Conversely, if the channel bandwidth of the measuring instrument is narrower than the *intrinsic* signal bandwidth then the measured power at sample frequency  $f_0$  is diluted by a factor of  $\Delta f_{meas}/\Delta f_{sig}$  relative to the total signal power. If the total signal power is required then the power contributions from an appropriate number of adjacent channels need to be summed.



**Mathematical Derivation** 

Combining equations (1) and (3):

$$P_{\text{meas}}(f_0) \approx \begin{cases} \frac{P_{\text{sig}}}{\Delta f_{\text{sig}}} \int_{f_0 - \frac{\Delta f_{\text{sig}}}{2}}^{f_0 + \frac{\Delta f_{\text{sig}}}{2}} df = P_{\text{sig}} & \Delta f_{\text{sig}} \leq \Delta f_{\text{meas}} \\ \frac{P_{\text{sig}}}{\Delta f_{\text{sig}}} \int_{f_0 - \frac{\Delta f_{\text{meas}}}{2}}^{f_0 + \frac{\Delta f_{\text{meas}}}{2}} df = \left(\frac{\Delta f_{\text{meas}}}{\Delta f_{\text{sig}}}\right) \cdot P_{\text{sig}} & (\langle P_{sig} \rangle) \left(\Delta f_{\text{sig}} > \Delta f_{\text{meas}}\right) \end{cases}$$
(5)

which can be simplified to:

$$P_{\text{meas}}(f_0) \approx \min\left(1, \frac{\Delta f_{\text{meas}}}{\Delta f_{\text{sig}}}\right) P_{\text{sig}} \quad [W]$$
 (6)

If the channel bandwidth of the measuring instrument is wider than the *intrinsic* signal bandwidth then the measured power at sample frequency  $f_0$  is equal to the total power of the signal, and independent of the channel bandwidth. Conversely, if the channel bandwidth of the measuring instrument is narrower than the *intrinsic* signal bandwidth then the measured power at sample frequency  $f_0$  is diluted by a factor of  $\Delta f_{meas}/\Delta f_{sig}$  relative to the total signal power. If the total signal power is required then the power contributions from an appropriate number of adjacent channels need to be summed.



**Mathematical Derivation** 

$$P_{N} = k T_{sys} \Delta f_{meas}$$

$$\sigma = \frac{k T_{sys} \Delta f_{meas}}{\sqrt{\Delta f_{meas} t_{i}}}$$

The noise floor of the measurement device is proportional to the measurement bandwidth (RBW for a spectrum analyzer), and the statistical fluctuations of the noise floor are proportional to the square-root of the measurement bandwidth. Using this information together with equation (6), the signal-to-noise ratio (SNR) for the measurement of a signal spectrum has this dependence on the measurement bandwidth:

$$\operatorname{SNR} \propto \frac{\min\left(1, \frac{\Delta f_{\text{meas}}}{\Delta f_{\text{sig}}}\right)}{\sqrt{\Delta f_{\text{meas}}}} = \begin{cases} \sqrt{\Delta f_{\text{meas}}} / \Delta f_{\text{sig}} & \left(<1/\sqrt{\Delta f_{\text{sig}}}\right) & \Delta f_{\text{meas}} < \Delta f_{\text{sig}} \\ 1/\sqrt{\Delta f_{\text{sig}}} & \Delta f_{\text{meas}} = \Delta f_{\text{sig}} \\ 1/\sqrt{\Delta f_{\text{meas}}} & \left(<1/\sqrt{\Delta f_{\text{sig}}}\right) & \Delta f_{\text{meas}} > \Delta f_{\text{sig}} \end{cases}$$
(7)

The SNR for the transition case where  $\Delta f_{\text{meas}} = \Delta f_{\text{sig}}$ , i.e. when the measurement bandwidth if *matched* to the signal bandwidth. This is **always** the optimal measurement configuration for detecting spectral line components of signals and measuring their power or PSD.



#### **Mathematical Derivation**

The measured PSD is defined to be:

$$PSD_{\text{meas}}(f_0) = \frac{P_{\text{meas}}(f_0)}{\Delta f_{\text{meas}}} \quad [W/Hz]$$
(8)

which when combined with equation (6) results in:

$$PSD_{\text{meas}}(f_0) \approx \frac{\min\left(1, \frac{\Delta f_{\text{meas}}}{\Delta f_{\text{sig}}}\right) P_{\text{sig}}}{\Delta f_{\text{meas}}} \quad [W/Hz]$$
(9)

Multiplying the numerator and denominator by  $\Delta f_{sig} / \Delta f_{meas}$ :

$$PSD_{\text{meas}}(f_0) \approx \frac{\min\left(\frac{\Delta f_{\text{sig}}}{\Delta f_{\text{meas}}}, 1\right) P_{\text{sig}}}{\Delta f_{\text{sig}}} = \min\left(\frac{\Delta f_{\text{sig}}}{\Delta f_{\text{meas}}}, 1\right) PSD_{\text{sig}} \quad [W/\text{Hz}]$$
(10)

If  $\Delta f_{meas} < \Delta f_{sig}$  then the *intrinsic* spectrum is *resolved* and the measured PSD is equal to the intrinsic signal PSD. Conversely, when  $\Delta f_{meas} > \Delta f_{sig}$  the spectrum is smeared out by the convolution with the channel bandpass response, and is diluted by a factor  $\Delta f_{sig}/\Delta f_{meas}$ . Unless the intrinsic signal is known, it is not possible to estimate the intrinsic signal PSD from the measured spectrum.



**Mathematical Derivation** 

The SKA and SARAS RFI regulations specify signal spectral density thresholds to be met for particular channel bandwidths, specified as fractional bandwidths about a given centre frequency, i.e.  $\Delta f_{thresh} = 0.01f_0$  for the Continuum threshold and  $\Delta f_{thresh} = 0.00001f_0$  for the Spectral Line threshold. It is not always practical or possible (or even desirable if the measurement SNR is to be optimised) to measure the RFI signal PSD at the specified channel bandwidth, so it is necessary to understand the relationship between the PSD determined using a channel bandwidth of  $\Delta f_{meas}$  and the compliance PSD defined using a specified bandwidth of  $\Delta f_{thresh}$ . Equation (10) can be recast in terms of the required channel bandwidth associated with the RFI threshold:

$$PSD_{\text{thresh}}(f_0) \approx \min\left(\frac{\Delta f_{\text{sig}}}{\Delta f_{\text{thresh}}}, 1\right) PSD_{\text{sig}} \quad [W/\text{Hz}]$$
 (11)



**Mathematical Derivation** 

When comparing the measured PSD in equation (10) to the threshold PSD in equation (11):

$$PSD_{\text{meas}}(f_0) \approx \eta \times PSD_{\text{thresh}}(f_0)$$
 (12)

where the scaling factor is referred to as the bandwidth compensation factor ( $\eta$ ):

$$\eta = \frac{\min\left(\frac{\Delta f_{\text{sig}}}{\Delta f_{\text{meas}}}, 1\right)}{\min\left(\frac{\Delta f_{\text{sig}}}{\Delta f_{\text{thresh}}}, 1\right)}$$
(13)



### **Mathematical Derivation**

In [9] it is shown that an alternative to scaling and/or smoothing the measured PSDs for comparison with threshold levels would be to compare the measured PSD against two threshold levels: the original threshold level and a scaled level that compensates for the bandwidth effects, i.e.

$$PSD_{comp} = PSD_{thresh} \times \left(\frac{\Delta f_{thresh}}{\Delta f_{meas}}\right)$$
(14)

Measured signal spectrum components that are **lower** than the **more conservative** threshold level is an **uncontested compliance**, and signal components that **exceed** the **more lenient** threshold level is an **uncontested non-compliance**.

Signal components that fall between the two threshold levels could be examined on a case-by-case basis, taking the measured or *a priori* signal bandwidth into account when making a compliance judgement.



# Measurement Case Study

### **EMI Measurements**



**Figure 4**: (Top) Measured PSD for RBW=120 kHz (blue trace) and RBW = 500 Hz (red trace); (Bottom) Integrated PSD to equivalent Continuum RBW = 1%·f<sub>c</sub>



# Measurement Case Study

#### **EMI Measurements**



**Figure 5:** Measured PSD (light blue trace) with RBW = 120 kHz and Integrated PSD (magenta trace) for a DUT at R = 10m from the receiver in a shielded enclosure of 80 dB compared to Continuum and Bandwidth Compensated Spectral Line Thresholds.



# Measurement Case Study

#### **EMI Measurements**



**Figure 6:** Measured PSD (light blue trace) with RBW = 500 Hz and Integrated PSD (magenta trace) for a DUT at R = 10m from the receiver in a shielded enclosure of 80 dB compared to Continuum and Bandwidth Compensated Spectral Line Thresholds.



### CONCLUSIONS

I. Haywood, F. Camilo et. al., Inflation of 430-parsec bipolar radio bubbles in the Galactic Centre by an energetic event, Nature, Vol. 573, pp. 235-237, 11 Sept. 2019

## Conclusions

When characterising emissions from a DUT and determining the impact on a radio telescope receiver, the following bandwidths need to be considered:

a. Interference signal bandwidths:  $\Delta f_{sig}$ 

(for example a narrowband or wideband interference signal)

- b. Measurement receiver bandwidths:  $\Delta f_{meas}$ (for example using a spectrum analyser with an RBW of 120 kHz as per CISPR 22 Class B, or RTA-3.6 channel width of 25 kHz)
- c. Radio astronomy protection levels bandwidths:  $\Delta f_{\rm thresh}$ (1% or 0.001% of the centre frequency for Continuum or Spectral Line observations respectively)

$$\eta = \frac{\min\left(\frac{\Delta f_{\text{sig}}}{\Delta f_{\text{meas}}}, 1\right)}{\min\left(\frac{\Delta f_{\text{sig}}}{\Delta f_{\text{sig}}}, 1\right)}$$





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The South African Radio Astronomy Observatory (SARAO) is a National Facility managed by the National Research Foundation and incorporates all national radio astronomy telescopes and programmes. SARAO is responsible for implementing the Square Kilometre Array (SKA) in South Africa.

### **Contact information**

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